

MAQAO Performance Analysis and Optimization Tool



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PeXL

UNIVERSITÉ

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Performance analysis and optimisation

How much can I optimise my application?

- Can it actually be done?
- What would the effort/gain ratio be?

Where can I gain time?

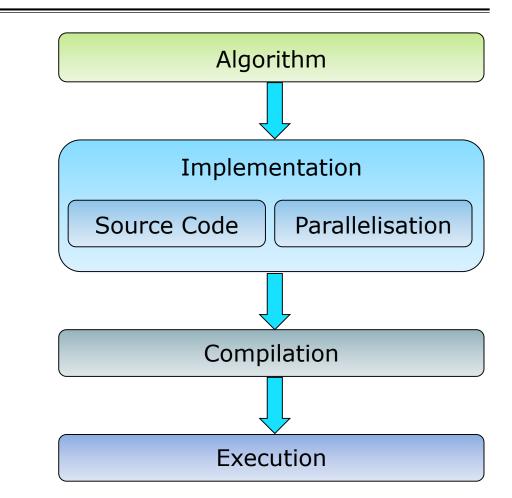
Where is my application wasting time?

Why is the application spending time there?

- Algorithm, implementation or hardware?
- Data access or computation?

How can I improve the situation?

- In which step(s) of the design process?
- What additional information do I need?



A multifaceted problem

Pinpointing the performance bottlenecks

Identifying the dominant issues

Algorithms, implementation, parallelisation, ...

Making the **best use** of the machine features

- Complex multicore and manycore CPUs
- Complex memory hierarchy

Finding the **most rewarding** issues to be fixed

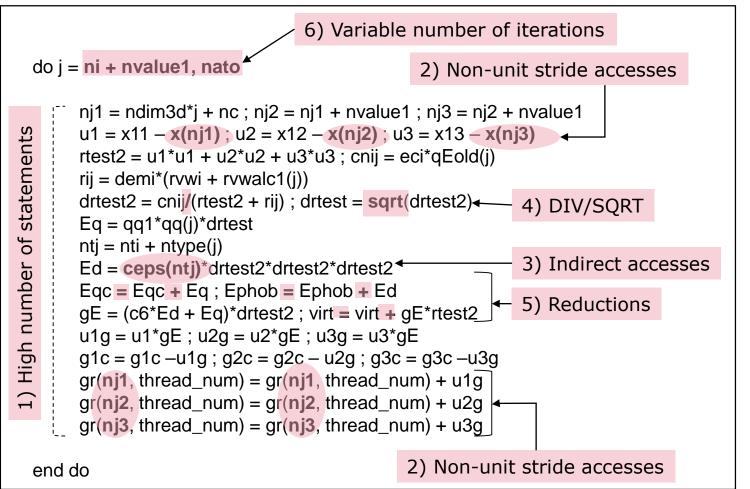
- 40% total time, expected 10% speedup
 - ➡ TOTAL IMPACT: 4% speedup
- 20% total time, expected 50% speedup
 - → TOTAL IMPACT: 10% speedup



➔ Need for dedicated and complementary tools

Motivating example

Code of a loop representing ~10% walltime



Source code and associated issues:

- 1) High number of statements
- 2) Non-unit stride accesses
- 3) Indirect accesses
- 4) DIV/SQRT
- 5) Reductions
- 6) Variable number of iterations

MAQAO: Modular Assembly Quality Analyzer and Optimizer

Objectives:

- Characterizing performance of HPC applications
- Focusing on performance at the core level
- Guiding users through optimization process
- Estimating return of investment (R.O.I.)

Characteristics:

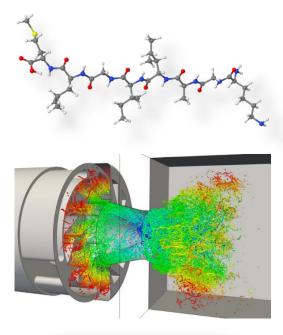
- Modular tool offering complementary views
- Support for Intel x86-64 and Xeon Phi
 - ARM under development
- LGPL3 Open Source software
- Developed at UVSQ since 2004
- Binary release available as static executable

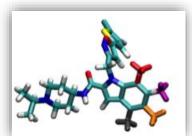


Success stories

MAQAO was used for optimizing industrial and academic HPC applications:

- QMC=CHEM (IRSAMC)
 - Quantum chemistry
 - Speedup: > 3x
 - Moved invocation of function with identical parameters out of loop body
- Yales2 (CORIA)
 - Computational fluid dynamics
 - Speedup: up to 2.8x
 - Removed double structure indirections
- Polaris (CEA)
 - Molecular dynamics
 - Speedup: 1.5x 1.7x
 - Enforced loop vectorisation through compiler directives
- AVBP (CERFACS)
 - Computational fluid dynamics
 - Speedup: **1.08x 1.17x**
 - Replaced division with multiplication by reciprocal
 - Complete unrolling of loops with small number of iterations





Partnerships

MAQAO was funded by UVSQ, Intel and CEA (French department of energy) through Exascale Computing Research (ECR) and the French Ministry of Industry through various FUI/ITEA projects (H4H, COLOC, PerfCloud, ELCI, etc...)

Provides core technology to be integrated with other tools:

- TAU performance tools with MADRAS patcher through MIL (MAQAO Instrumentation Language)
- ATOS bullxprof with MADRAS through MIL
- Intel Advisor
- INRIA Bordeaux HWLOC

PeXL ISV also contributes to MAQAO:

- Commercial performance optimization expertise
- Training and software development
- www.pexl.eu









MAQAO team and collaborators

- Prof. William Jalby
- Prof. Denis Barthou
- Prof. David J. Kuck
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- Jean-Thomas Acquaviva, Ph D
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- Julien Jaeger, Ph D
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- Cédric Valensi, Ph D
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- Zakaria Bendifallah, Ph D
- Emmanuel Oseret, Ph D
- Pablo de Oliveira, Ph D

- Tipp Moseley, Ph D
- David C. Wong, Ph D
- Jean-Christophe Beyler, Ph D
- <u>Mathieu Tribalat</u>
- <u>Hugo Bolloré</u>
- Jean-Baptiste Le Reste
- Sylvain Henry, Ph D
- Salah Ibn Amar
- Youenn Lebras
- Othman Bouizi, Ph D
- José Noudohouenou, Ph D
- Aleksandre Vardoshvili
- Romain Pillot

Analysis at binary level

Advantages of binary analysis:

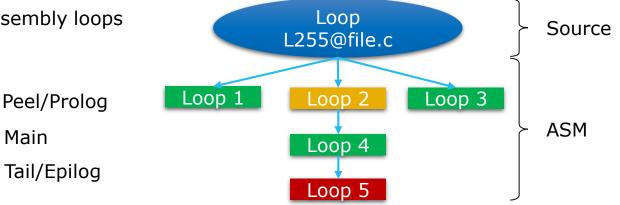
- Compiler optimizations increase the distance between the executed code and the source
- Source code instrumentation may prevent the compiler from applying some transformations

Main

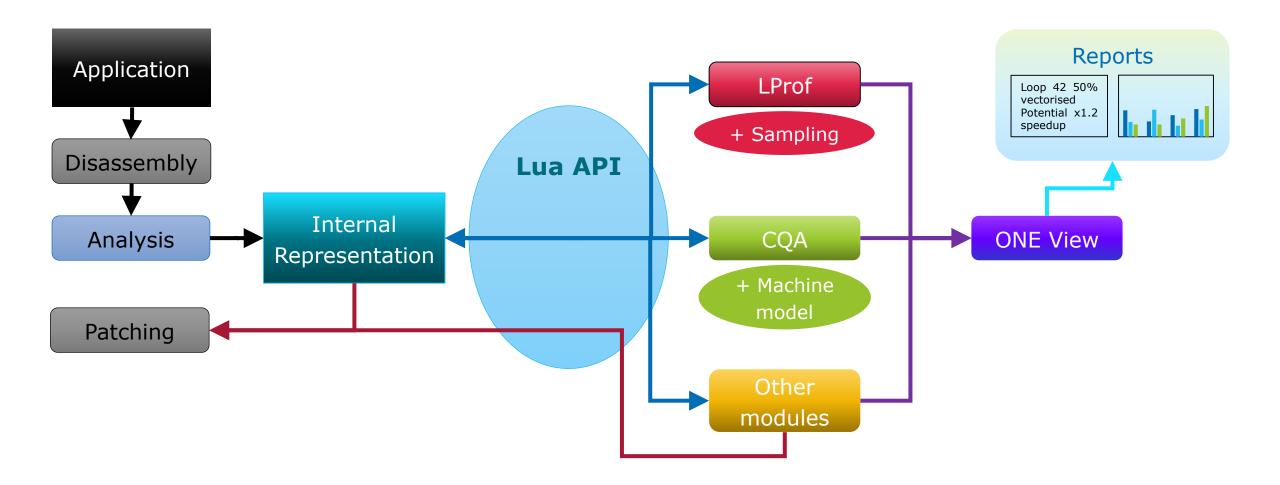
We want to evaluate the "real" executed code: What You Analyse Is What You Run

Main steps:

- Reconstruct the program structure
- Relate the analyses to source code
 - A single source loop can be compiled as multiple assembly loops
 - Affecting unique identifiers to loops

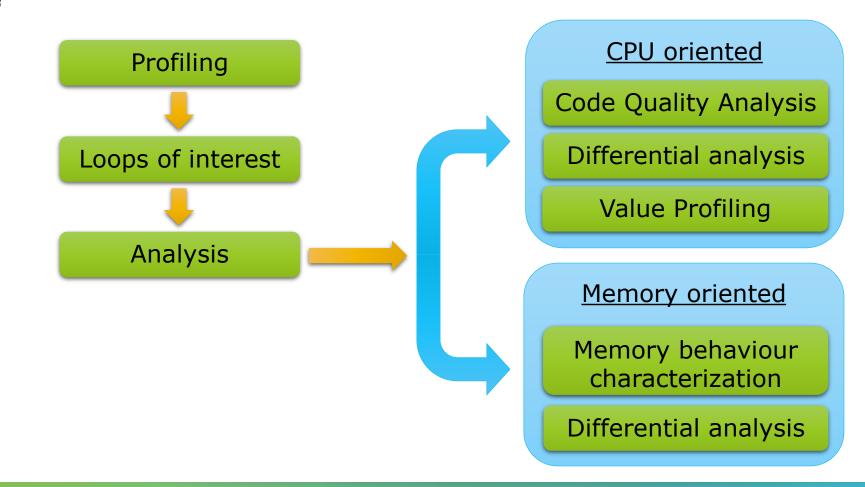


MAQAO Main structure



MAQAO Methodology

Decision tree



MAQAO LProf: Lightweight Profiler

Goal: Lightweight localization of application hotspots

Features:

- Sampling based
- Access to hardware counters for additional information
- Results at function and loop granularity

Strengths:

• Non intrusive: No recompilation necessary

Low overhead

Agnostic with regard to parallel runtime

MACAO Global Application Functions

Loops Help

unctions and Loops

Right-click on a line to display the associated load balancing. Double click on a loop to display its analysis details.

Name					Module	Coverage (%)	Time (s)	Nb Threads	Deviation
 binvcrhs 					bt-mz.C.16	23.19	13.66	64	1.73
▼ y_solve					bt-mz.C.16	13.09	7.71	64	1.08
▼ Loop 204 - y_solve.f:53-407 - bt-mz.C.16						12.84	7.56		
Loop 205 - y_solve.f:54-407 - bt-mz.C.16						12.84	7.56		
▼ Loop 207 - y_solve.f:54-398 - bt-mz.C.16						12.84	7.56		
 Loop 211 - y_solve.f:145-307 - bt-mz.C.16 						7.06	4.16		
 Loop 213 - y_solve.f:55-137 - bt-mz.C.16 						4.43	2.61		
 Loop 206 - y_solve.f:394-398 - bt-mz.C.16 						0.88	0.52		
 Loop 209 - y_solve.f:337-360 - bt-mz.C.16 						0.33	0.19		
 Loop 210 - y_solve.f:145-307 - bt-mz.C.16 						0.09	0.05		
 Loop 212 - y_solve.f:55-137 - bt-mz.C.16 						0.05	0.03		
► x_solve					bt-mz.C.16	12.49	7.35	64	1.02
 _INTERNAL_25src_kmp_barrier_cpp_ce635104::_ kmp_info*, int, int, int, void*) 	kmp_hyper	_barrier_	release(barrier_	type,	libiomp5.so	12.36	7.28	64	8.22
▶ matmul_sub					bt-mz.C.16	11.95	7.04	64	0.92
► z_solve					L	0.00	4 70	~ •	0.57
▶ compute_rhs					bt-mz.C.16 - Loo	p 211			
▶ matvec_sub									
 MPIDI_CH3I_Progress 	Т								
 binvrhs 					1 . 1				
► Ihsinit	7-								
► add#omp_loop_0		_							
 system_call_after_swapgs 	6-								
 _INTERNAL_25src_kmp_barrier_cpp_ce635104; 	۰-								
kmp_info*, int, int, void (*)(void*, void*), void*)									
 sysret_check 	5-								
◦kmp_yield	Loverage								
 apic_timer_interrupt 	4-								
copy_x_face#omp_loop_0	8								
► exact_solution	3-								
 update_curr 	Ŭ								
 audit_syscall_entry 									
 schedule 	2-								
 task_tick_fair 									
► copy_y_face#omp_loop_0	1-								
 cpuact_charge 									
					<u> </u>	<u> </u>			
 intel_pstate_update_util ktime_get 	0 30872	30954	30937 30983	30877	30942 30971 30976	30882 3	30940 309	87 30981	30887

MAQAO CQA: Code Quality Analyzer

Goal: Assist developers in improving code performance

Features:

- Evaluates the **quality** of the compiler generated code
- Returns hints and workarounds to improve quality
- Focuses on loops
 - In HPC most of the time is spent in loops
- Targets compute-bound codes

Static analysis:

- Requires no execution of the application
- Allows cross-analysis

Static Reports

▼ CQA Report

The loop is defined in /tmp/NPB3.3.1-MZ/NPB3.3-MZ-MPI/BT-MZ/z_solve.f:415-423

▼ Path 1

2% of peak computational performance is used (0.77 out of 32.00 FLOP per cycle (GFLOPS @ 1GHz)) gain potential hint expert

Code clean check

Detected a slowdown caused by scalar integer instructions (typically used for address computation). By removing them, you can lower the cost of an iteration from 65.00 to 57.00 cycles (1.14x speedup).

Workaround

- Try to reorganize arrays of structures to structures of arrays
- Consider to permute loops (see vectorization gain report)
- To reference allocatable arrays, use "allocatable" instead of "pointer" pointers or qualify them with the "contiguous" attribute (Fortran 2008)
- For structures, limit to one indirection. For example, use a_b%c instead of a%b%c with a_b set to a%b before this loop

Vectorization

Your loop is not vectorized. 8 data elements could be processed at once in vector registers. By vectorizing your loop, you can lower the cost of an iteration from 65.00 to 8.12 cycles (8.00x speedup).

Workaround

- Try another compiler or update/tune your current one:
- use the vec-report option to understand why your loop was not vectorized. If "existence of vector dependences", try the IVDEP directive. If, using IVDEP, "vectorization possible but seems inefficient", try the VECTOR ALWAYS directive.
- Remove inter-iterations dependences from your loop and make it unit-stride:
 - If your arrays have 2 or more dimensions, check whether elements are accessed contiguously and, otherwise, try to permute loops accordingly: Fortran storage order is column-major: do i do j a(i,j) = b(i,j) (slow, non stride 1) => do i do j a(j,i) = b(i,j) (fast, stride 1)
 - If your loop streams arrays of structures (AoS), try to use structures of arrays instead (SoA): do i a(i)%x = b(i)%x (slow, non stride 1) => do i a%x(i) = b%x(i) (fast, stride 1)

Execution units bottlenecks

Found no such bottlenecks but see expert reports for more complex bottlenecks.

MAQAO CQA: Main Concepts

Most of the time, applications only exploit at best 5 to 10% of the peak performance.

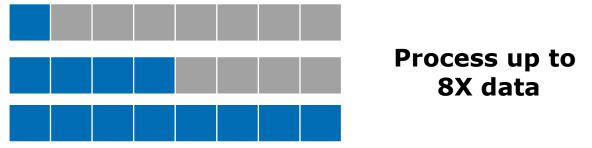
Main elements of analysis:

- Peak performance
- Execution pipeline
- Resources/Functional units

Key performance levers for core level efficiency:

- Vectorizing
- Avoiding high latency instructions if possible
- Having the compiler generate an efficient code
- Reorganizing memory layout

Same instruction – Same cost



MAQAO CQA: Compiler and programmer hints

Compiler can be driven using flags and pragmas:

- Ensuring full use of architecture capabilities (e.g. using flag -xHost on AVX capable machines)
- Forcing optimization (unrolling, vectorization, alignment, ...)
- Bypassing conservative behaviour when possible (e.g. 1/X precision)

Implementation changes:

- Improve data access
 - Loop interchange
 - Changing loop strides
 - Reshaping arrays of structures
- Avoid instructions with high latency

MAQAO ONE View: Performance View Aggregator

Automating the whole analysis process

- Invocation of the required MAQAO modules
- Generation of aggregated performance views available as HTML files

Main steps:

- Invokes LProf to identify hotspots
- Invokes CQA on loop hotspots

Available results:

- Speedup predictions
- Global code quality metrics
- Hints for improving performance
- Parallel efficiency



Analysing an application with MAQAO

Execute ONE View

- Provide all parameters necessary for executing the application
 - Parameters can be passed on the command line or into a configuration file
 - Parameters include binary name, MPI commands, dataset directory, ...

```
$ maqao oneview --create-report=one --binary=bt-mz.C.16 --mpi command="mpirun -n 16"
```

- Analyses can be tweaked if necessary
 - Report one corresponds to profiling and code quality analysis
- ONE View can reuse an existing experiment directory to perform further analyses
- Results available in HTML by default
 - XLS files or console output available

Help and tutorials available on the MAQAO website: www.maqao.org/documentation.html

Analysing an application with MAQAO

MAQAO modules can be invoked separately for advanced analyses

- LProf
 - Profiling

```
$ maqao lprof xp=exp_dir --mpi-command="mpirun -n 16" -- ./bt-mz.C.16
```

Display

```
$ maqao lprof xp=exp_dir -df
```

Displaying the results from a ONE View run

```
$ maqao lprof xp=oneview_xp_dir/lprof_npsu -df
```

CQA

\$ maqao cqa loop=42 bt-mz.C.16

Help and tutorials available on the MAQAO website: www.maqao.org/documentation.html

Global summary

Experiment summary

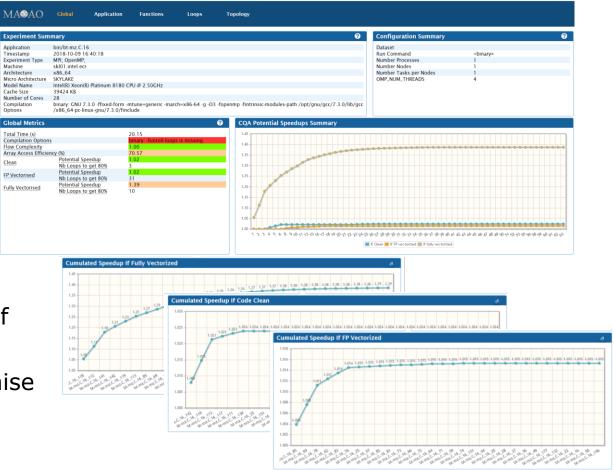
 Characteristics of the machine where the experiment took place

Global metrics

- General quality metrics derived from MAQAO analyses
- Global speedup predictions

CQA potential speedups

- Speedup prediction depending on the number of vectorised loops
- Ordered speedups to identify the loops to optimise in priority



Application Characteristics

Application categorisation

- Time spent in different regions of code
- Function based profile
- Functions by coverage ranges

Loop based profile

Loops by coverage ranges

Detailed loop based profile

Loop types by coverage ranges

Loop Resed Profile



Application Characteristics: Time Categorisation

Identifying at a glance where time is spent

- Application
 - Main executable
- Parallelization
 - Threads
 - OpenMP
 - MPI
- System libraries
 - I/O operations
 - String operations
 - Memory management functions
- External libraries
 - Specialised libraries such as libm / libmkl
 - Application code in external libraries

∕IA € AO	Global	Application	Functions	Loops	Help
pplication Categ	jorization				
		86%			OMP Binary MPI
			11%		Memory System

Functions Profiling

Identifying hotspots

- Exclusive coverage
- Load balancing across threads
- Loops nests by functions

- ▼ matmul_sub
 - Loop 230 solve_subs.f:71-175 bt-mz.C.16
 - Loop 231 solve_subs.f:71-175 bt-mz.C.16
- ▼ z_solve

Loop 232 - z_solve.f:53-423 - bt-mz.C.16

- Loop 233 z_solve.f:54-423 bt-mz.C.16
 - Loop 236 z_solve.f:54-423 bt-mz.C.16
 - Loop 239 z_solve.f:146-308 bt-mz.C.16 Innermost

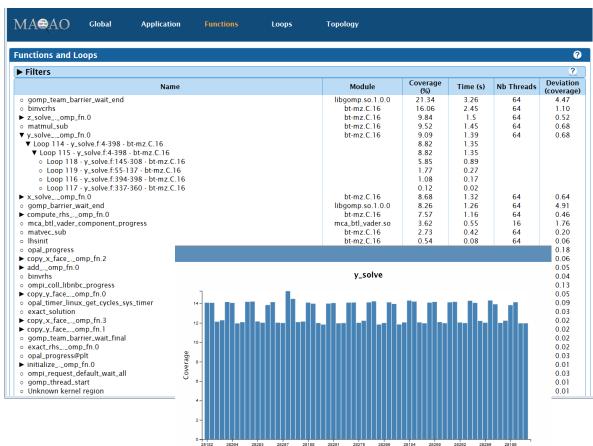
Single

Outermost

Inbetween

Inbetween

- Loop 235 z_solve.f:55-137 bt-mz.C.16
- Loop 234 z_solve.f:415-423 bt-mz.C.16



Loops Profiling Summary

Identifying loop hotspots

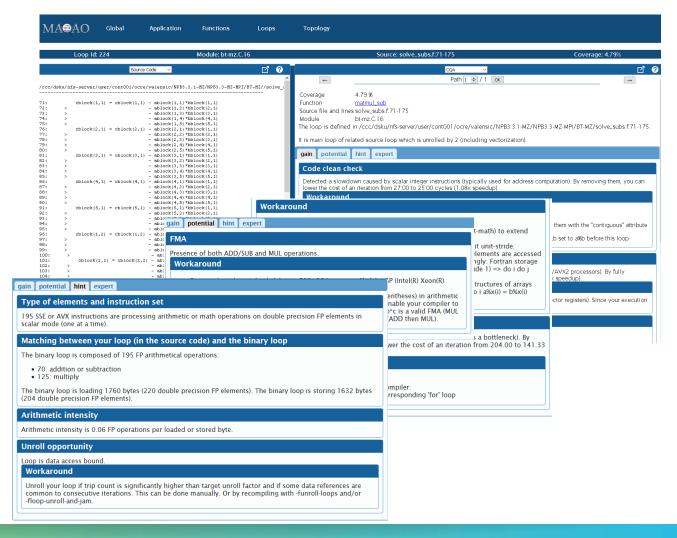
- Vectorisation information
- Potential speedups

ЛА <mark>Q</mark>	AO	Global Applicatio	on Functions	Loops	Help			
oops In	dex							
		to display its analysis deta ics above the table to displ						
✓ Cove	rage (%)	✓Vectorization Ratio (%)	☑ Speedup If Clean	⊠Speedup If F		edup If Fully Ve		
Loop id	Source Lines	Source File	Source Function	Coverage (%)	Vectorization Ratio (%)	Speedup If Clean	Speedup If FP Vectorized	Speedup If Fully Vectorized
Loop 211	145-307	bt-mz.C.16:y_solve.f	y_solve	7.06	45.13	1	1.22	5.52
Loop 201	146-308	bt-mz.C.16:x_solve.f	x_solve	7.06	45.13	1	1.22	5.52
Loop 230	71-175	bt-mz.C.16:solve_subs.f	matmul_sub	5.57	100	1.02	1.9	4
Loop 213	55-137	bt-mz.C.16:y_solve.f	y_solve	4.43	47	1.05	1.16	5.93
Loop 203	57-139	bt-mz.C.16:x_solve.f	x_solve	3.93	48.36	1.01	1.09	5.83
Loop 239	146-308	bt-mz.C.16:z_solve.f	z_solve	3.06	8.97	1.07	1.8	8
Loop 235	55-137	bt-mz.C.16:z_solve.f	z_solve	2.81	22.08	1.03	1.62	7.49
Loop 234	415-423	bt-mz.C.16:z_solve.f	z_solve	1.54	0	1.14	1.67	8
Loop 122	304-349	bt-mz.C.16:rhs.f	compute_rhs	1.32	71.26	1.33	1.92	5.36
Loop 148	194-238	bt-mz.C.16:rhs.f	compute_rhs	1.25	71.59	1.32	1.93	5.38
Loop 162	83-132	bt-mz.C.16:rhs.f	compute_rhs	1.23	71.59	1.24	1.87	5.26
Loop 231	71-175	bt-mz.C.16:solve_subs.f	matmul_sub	1.11	10.59	1	2.29	8
Loop 227	23-27	bt-mz.C.16:solve_subs.f	matvec_sub	0.97	100	1	1.95	4
Loop 206	394-398	bt-mz.C.16:y_solve.f	y_solve	0.88	0	1.04	1.73	8
Loop 196	395-399	bt-mz.C.16:x_solve.f	x_solve	0.84	0	1.04	2.02	8
Loop 229	23-27	bt-mz.C.16:solve_subs.f	matvec_sub	0.62	100	1	1.95	4
Loop 170	40-50	bt-mz.C.16:rhs.f	compute_rhs	0.4	73.33	1	1.82	4
Loop 105	388-391	bt-mz.C.16:rhs.f	compute_rhs	0.35	100	1.12	1.83	4
Loop	313-314	bt-mz.C.16:z_solve.f	z_solve	0.35	0	1	1	8

Loop Analysis Reports

High level reports

- Reference to the source code
- Bottleneck description
- Hints for improving performance
- Reports categorized by probability that applying hints will yield predicted gain
 - Gain: Good probability
 - Potential gain: Average probability
 - Hints: Lower probability



Loop Analysis Reports – Expert View

Hide grou analysi 0x424e35 MO¹ 0x424e35 MO¹ 0x424e3c MUI 0x424e40 LEA 0x424e48 SUE 0x424e48 SUE 0x424e44 LEA

0x424e5e MOV 0x424e62 MUI 0x424e66 MOV 0x424e6e SUE 0x424e73 MOV 0x424e78 MUI 0x424e7c SUE

0x424e8e MUI 0x424e92 SUE

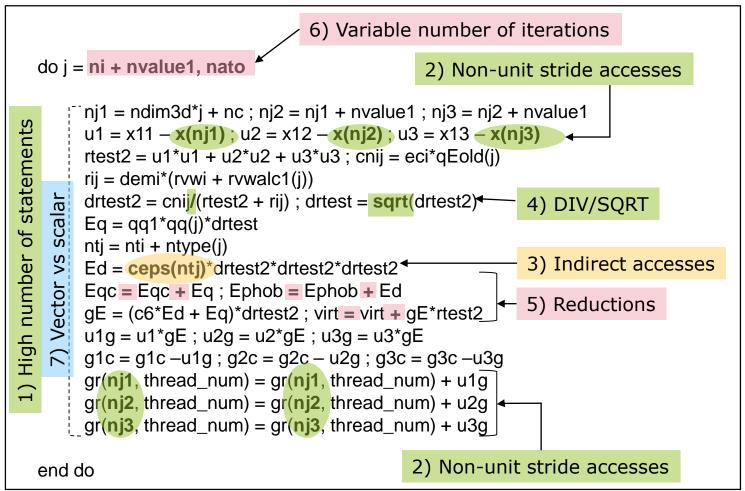
Low level reports for performance experts

- Assembly-level
- Instructions cycles costs
- Instructions dispatch predictions
- Memory access analysis

	Gain Potential gain Hints Exp	perts only	y										
perts				ASM	l code								
perts	In the binary file, the address of the lo	op is: 421	409	ASIV	rcoue								
	Instruction	Nb FU	J PO	P1	P2	P3	P4	P5	P6	Latency	Recip. thre	oughput	
	MOVAPS %XMM13,%XMM5	1	0.50	0.50	0	0	0	0	0	2	0.50		
	INC %RDI	1	0	0	0	0	1.50	0.50	0	1	1		
	DIVSD 0x28(%R10,%RDX,1),%XMM5	4	1	0	0.50	0.50	0	0	0	40-42	12-32		
	MOVAPS %XMM5,%XMM15	1	0.50	0.50	0	0	0	0	0	2	0.50		
	MULSD %XMM5,%XMM15	1	0.50	0.50	0	0	0	0	0	6	0.50		
	MOVSD %XMM5,0x12890(%R14)	1	0	0	0.50		0	0	1	2	1		
	MULSD %XMM15,%XMM5	1	0.50	0.50	0	0	0	0	0	6	0.50		
	MOVSD %XMM15,0x12898(%R14)	1	0	0	0.50	0.50	0	0	1	2	1		
	MOVSD %XMM5,0x128a0(%R14)	1	0	0	0.50	0.50	0	0	1	2	1		
	MOVSD %XMM14,(%R9,%R14,1)	1	0	0	0.50	0.50	0	0	1	2	1		
	MOVSD %XMM14,0x28(%R9,%R14,1)	1	0	0	0.50	0.50		0	1	2	1		
) Id: 224	Module: bt-mz.C.16				Source:	solve_s	ubs.f:71-	175				Cove	erage: 4.79%
	Assembly Code V	2 6							604 A	dvanced v			
	Assembly Code 🗸	L L C	^	+	1					uvanceu	4		
				-	_				1 au	1 / !	<u>OK</u>		
	[0]						I	Metric					Value
' <mark>S (%RDI,%RAX,8),%XMM</mark> 4 S %XMM5,%XMM2	[3]			overage (9	6 app. tin	ne)						4.79	
%XMM4,%XMM2				ne (s))A speed	up if clo	-						0.23 1.08	
CX,%RAX,8),%RSI				2A speed 2A speed			orized					1.65	
S (%RSI),%XMM15 [2]				QA speed								2.00	
%XMM2,%XMM15			CC	A speed	up if no i	inter-itera	tion dep	endency				NA	
28(%RDI,%RAX,8),%R8 S (%R8) %XMM2 [4]		_		QA speed	up if ne×	t bottlene	eck killec	ł				1.08	
25 (% R8), % XMM2 [4] 25 0×1d0(% RSP), % XMM1	[1]			iurce iurce loop	- uproll -	ofo						solve_su unrolled	bs.f:71-175
PS %XMM12,%XMM14	Jan 19 1			urce loop urce loop			e level					max	Uý Z
D %XMM2,%XMM1				nroll/vect								main	
PS 0×130(%RSP),%XMM0	[1]			nroll facto								2	
%XMM1,%XMM15				QA cycles								27.00	
<u>'S 0×28(%R8),%XMM1</u> %XMM1,%XMM0				QA cycles								25.00	
%XMM0,%XMM15)A cycles)A cycles								16.32 13.50	
S 0×50(%R8),%XMM0				ont-end c		ectonzei						22.50	
PS 0xd0(%RSP),%XMM3	1]			cycles	,							25.00	
%ХММО,%ХММЗ				cycles								27.00	
%XMM3,%XMM15				cycles								13.00	
IPS 0×78(%R8),%XMM3			P3	cycles								13.00	

Application to Motivating Example

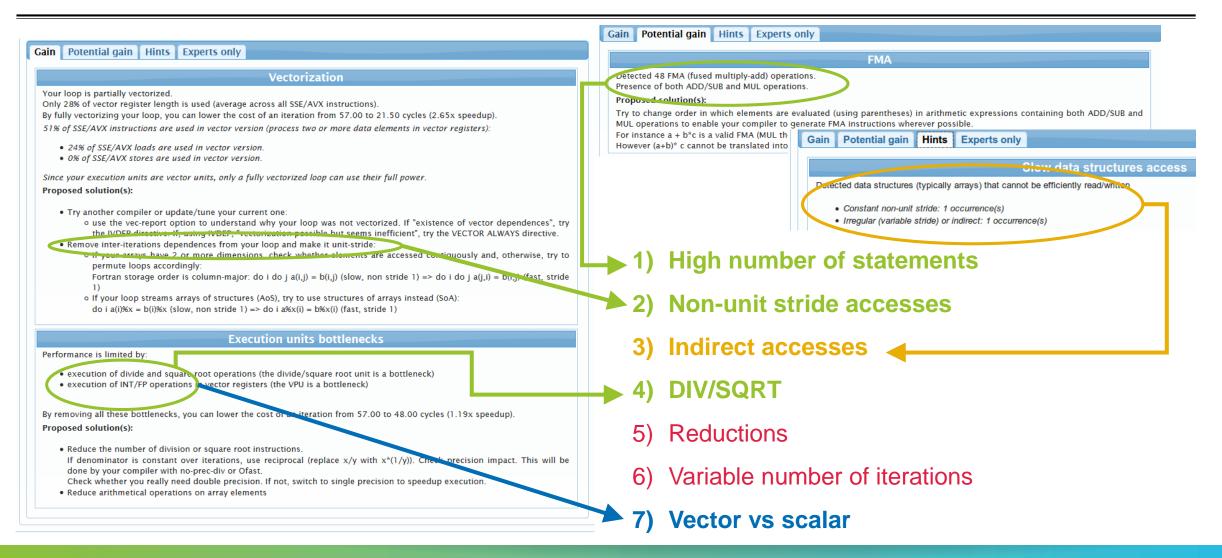
Issues identified by CQA



CQA can detect and provide hints to resolve most of the identified issues:

- 1) High number of statements
- 2) Non-unit stride accesses
- 3) Indirect accesses
- 4) DIV/SQRT
- 5) Reductions
- 6) Variable number of iterations
- 7) Vector vs scalar

Application to Motivating Example



MAQAO ONE View Thread/Process View

Software Topology

- Processes by node
- Thread by process

View by thread

Function profile at the thread or process level

AAAO Global Application Functions	Loops Topology	Help
ftware Topology		
ID		Time(s)
Node skylake01		11.22
▼ Process 359337		11.22
 Thread 359337 		11.22
Process 359338		11.16
Process 359352		11.22
Process 359351		11.2
Process 359353		11.22
Process 359354		11.22
Process 359355		11.18
Process 359356		11.18
Process 359357		11.22
Process 359358		11.18
Process 359359		11.18
Process 359360		11.16
Process 359361		11.18
Process 359362		11.08
Process 359364		11.22
Process 359366		11.19
AVERAGE		11.22

MAQAO	Global	Application	Functions	Loops	Topology	Help	
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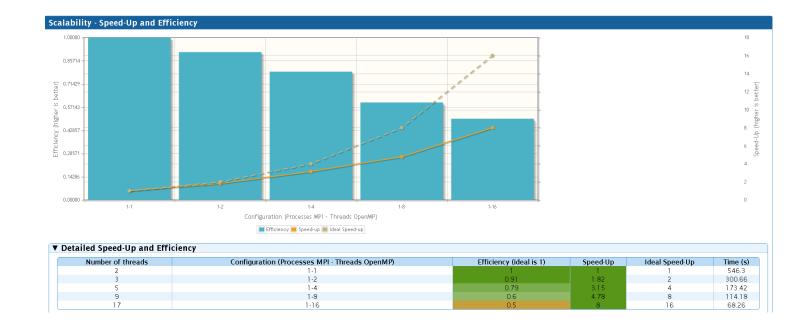
Profiling node skylake01 - process 359337 - thread 359337

Name	Module	Coverage (%)	Time (s)
 MPIDI_CH3I_Progress 	libmpi.so.12.0	20.62	2.31
▶ calc_data_gradient	3D_cylinder	4.95	0.56
ics_advance_velocity_tfv4a_4th	3D_cylinder	3.75	0.42
calc_data_tridiag_op_product	3D_cylinder	3.58	0.4
 MPIR_Allreduce_group 	libmpi.so.12.0	3.22	0.36
► filter_real_data	3D_cylinder	2.43	0.27
update_int_comm	3D_cylinder	2.42	0.27
 system_call_after_swapgs 	SYSTEM CALL	1.66	0.19
adv_scalar_w_u_tfv4a_4th	3D_cylinder	1.59	0.18
solve_linear_system_deflated_pcg	3D_cylinder	1.45	0.16

MAQAO ONE View Scalability Reports

Goal: Provide a view of the application scalability

- Profiles with different numbers of threads/processes
- Displays efficiency metrics for application



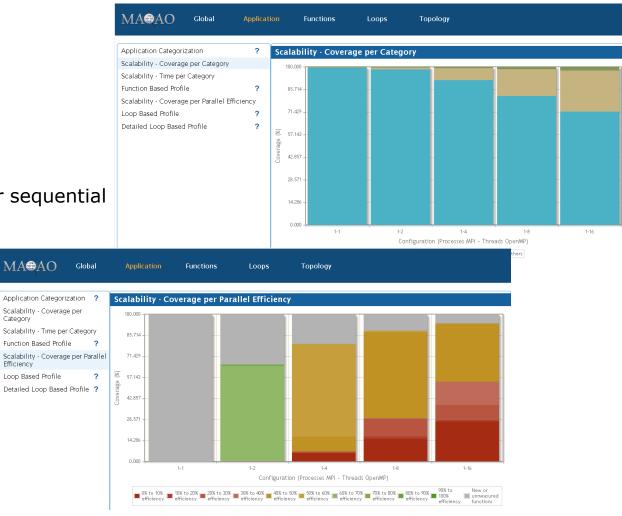
MAQAO ONE View Scalability Reports – Application View

Coverage per category

Comparison of categories for each run

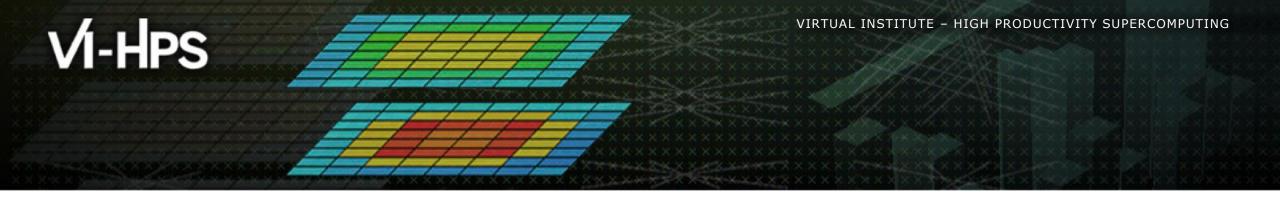
Coverage per parallel efficiency

- Efficiency = Tsequential / (Tparallel * Nthreads)
 - Distinguishing functions only represented in parallel or sequential
- Displays efficiency by coverage



MAQAO ONE View Scalability Reports – Functions and Loops Views

Displays metrics		MACAO Global Application Functions Loops Topology																				
			Functio	ons and Loops																0		
function/loop		► Filte											?									
rancelon, loop							otential Speed-) Potential Spe		2) Efficiency Select none	⊠(1-2) Pot	ential Speed-Up (%) ⊠(1-4)	Efficiency	☑(1-4) Pote	ntial Speed	-Up (%)	[] (1-8)	Efficiency	(1-8	8) Potentia	Speed-Up	(%)
 Efficiency 						Name			Module	Covera (%)	ge Time (s) N	Ib Threads	Deviation (coverage)	(1-1) Efficiency Ef	(1-2) Po ficiency S	(1-2) itential peed- Jp (%)		(1-4) Potential Speed- Up (%)		(1-8) Potential Speed- Up (%)	(1-16) Efficiency	(1-16) Potential Speed- Up (%)
 Potential speed 	up i	f ef	ficienc	y=1		ERNAL_25src_kmp per_barrier_release(barrier.	_barrier_cpp_a _type, kmp_inf		libiomp5.so	24.02	15.38	16	18.62		1	0	0.04	5.49	0.01	14.35	0.01	23
					 binv ▶ comp 				bt-mz.C.1 bt-mz.C.1	20.71 10.76	13.27	16 16	6.22 2.45	1		6.14 2.68	0.55 0.42	10.2 5.39	0.45 0.26	11.58 8.47	0.41 0.25	11.43 7.57
					P com	Juce_ma			Demi2.e.1	10.70	0.0	10	2.40			2.91	0.57	4.44	0.44	5.75	0.41	5.45
	MA	AO	Global App	lication Functio	ns L	oops Topology										2.69 2.48	0.55 0.55	4.24 3.73	0.42 0.46	5.43 4.09	0.37 0.41	5.61 4.18
																2.06	0.54 0.57	3.56 1.31	0.45 0.45	3.92 1.62	0.39	4.11 1.59
	Loops II	ndex													•	0.12	0.44	0.22	0.45	0.41	0.09	1.17
	☑(1-2	erage (%)) Efficiency ct none	□Time (s) □Vec ☑(1-2) Potential S		∃Speedup If C Efficiency	ency 🛛 (1-4) Potential Speed-Up (%) 🖓 (1-8) Efficiency 🖓 (1-8) Potential Speed-Up (%) 🖓 (1-16) Efficiency 🖓 (1-16) Potential Speed-Up (%)												0.62				
	Loop id	Fource	Source File	Source Function	(1-2) Efficiency	(1-2) Potential Speed- Up (%)	(1-4) Efficiency	(1-4) Potentia			I-8) Potential Spe			6) Potential S	peed-	0.1 0.11	0.57 0.56	0.27 0.2	0.53 0.51	0.24 0.19	0.42 0.44	0.31 0.21
	Loop	71-175	bt-mz.C.1:solve_sub	^s matmul sub	0.71	1.51	0.56	Up (% 2.49		iciency 0.45	Up (%) 2.99	Effici		Up (%) 2.96		0.06	1 0.27	0 0.15	0.07 0.14	0.24 0.27	0.04 0.11	0.34 0.3
	215 Loop 224		.t bt-mz.C.1:z_solve.f		0.7	1.34	0.57	2.07		0.43	2.73	0.		2.62		0.01 0.03	0.02 0.28	0.07 0.16	0.01 0.17	0.18 0.22	0 0.17	0.28 0.18
	Loop 192	146-308	bt-mz.C.1:x_solve.f	x_solve	0.66	1.22	0.52	1.91		0.45	1.92	0.3	9	2.04		0.07 0.07	0.48 0.21	0.1 0.16	0.31 0.14	0.16 0.2	0.37 0.13	0.1 0.18
	Loop 199	145-307	bt-mz.C.1:y_solve.f	y_solve	0.69	1.09	0.54	1.81		0.45	1.99	0.3	9	2.11		0	0.04	0.04	0.01	0.13	0.01	0.19 0.16
	Loop 169	40-50	bt-mz.C.1:rhs.f	compute_rhs	0.52	0.49	0.23	1.59		0.11	2.95	0.1	1	2.3		0.03 0.01	0.64 0.08	0.03 0.02	0.39	0.07	0.43 0.01	0.05 0.12
	Loop 221	55-137	bt-mz.C.1:z_solve.f	z_solve	0.66	0.92	0.54	1.32		0.43	1.56	0.3	37	1.66		0 0	0.06 0.06	0.02 0.02	0.02 0.02	0.06 0.05		0.07
	Loop 189	57-139	bt-mz.C.1:x_solve.f	x_solve	0.71	0.7	0.57	1.14		0.47	1.28	0.4	13	1.26		0	0.12	0.01	0.06	0.02 0.04		0.06
	Loop 196	55-137	bt-mz.C.1:y_solve.f	y_solve	0.73	0.52	0.55	1.01		0.44	1.18	0.4	u 👘	1.12		0	0.25 0.25	0.01	0.06	0.02		0.07
	Loop 165	65-67	bt-mz.C.1 :rhs.f	compute_rhs	0.45	0.55	0.24	1.22		0.11	2.31	0.1	3	1.64		0	0.25	0.02	0.04	0.03	0.02	0.06
	Loop 227	26-28	bt-mz.C.1:add.f	add#omp_loop_0	0.64	0.12	0.44	0.22		0.25	0.4	0.0	9	1.14								
	Loop 220	415-423	bt-mz.C.1:z_solve.f	z_solve	0.67	0.34	0.49	0.62		0.34	0.87	0.	3	0.88								
	Loop 188		bt-mz.C.1:x_solve.f		0.62	0.5	0.56	0.57		0.44	0.69	0.4	n	0.65								
	Loop 216	71-175	bt-mz.C.1:solve_sub: .f	^s matmul_sub	0.77	0.23	0.62	0.41		0.48	0.54	0.	4	0.62								
	Loop	304-349	bt-mz.C.1:rhs.f	compute_rhs	0.71	0.29	0.65	0.34		0.46	0.56	0.4	14	0.5								



Thank you for your attention !

Questions ?

